

OPTIMIZING EFFICIENCY AND PERFORMANCE IN 5G NETWORKS THROUGH A DYNAMIC RESOURCE ALLOCATION ALGORITHMIC FRAMEWORK

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Abstract

With the exponential growth of data demand and the advent of 5G networks, the need for efficient resource allocation algorithms has become paramount. This study presents a dynamic resource allocation algorithmic framework aimed at optimizing efficiency and performance in 5G networks. The framework focuses on frequency reuse at the edges while employing fractional pilots for enhanced spectrum utilization. 5G networks promise unprecedented speeds and low latency, enabling a wide array of applications from IoT to augmented reality. However, the efficient allocation of resources remains a challenge, especially at the network edges where interference is high. Traditional static resource allocation schemes fail to adapt to dynamic network conditions, leading to suboptimal performance. The main challenge lies in effectively managing resources to meet the diverse demands of various applications while mitigating interference and maximizing spectral efficiency. The proposed framework employs a dynamic resource allocation algorithm that adapts to changing network conditions in real-time. Leveraging fractional pilots, the algorithm optimizes frequency reuse at the network edges, thereby enhancing spectral efficiency. The framework integrates stochastic learning for predictive analytics to anticipate resource demands and interference patterns. Simulation results demonstrate significant improvements in spectral efficiency and network performance compared to traditional static allocation methods. The utilization of fractional pilots effectively reduces interference, enabling higher throughput and lower latency, especially at the network edges. The dynamic nature of the algorithm ensures adaptability to varying traffic loads, leading to enhanced overall network efficiency.

Keywords:

5G Networks, Dynamic Resource Allocation, Fractional Pilots, Interference Management, Spectral Efficiency

1. INTRODUCTION

As the world moves towards the era of 5G networks, the demand for high-speed data transmission and low-latency communication has surged exponentially. This paradigm shift not only promises to revolutionize various industries but also poses unprecedented challenges in terms of efficient resource allocation and management [1]-[2]. Traditional network architectures struggle to cope with the dynamic and diverse demands of 5G applications, particularly at the network edges where interference and resource scarcity are prevalent.

5G networks are designed to support a multitude of use cases ranging from massive machine-type communications to ultra-reliable low-latency communications. However, the realization of these ambitious goals requires innovative approaches to overcome the limitations of existing network infrastructures [3]-[5]. Static resource allocation strategies, which allocate resources

uniformly across the network, fail to adapt to the dynamic nature of 5G environments, leading to suboptimal performance and inefficient spectrum utilization.

The primary challenges in 5G network optimization lie in effectively managing resources to meet the diverse requirements of different applications while ensuring efficient spectrum utilization and minimizing interference [6]. Additionally, the proliferation of connected devices and the exponential growth of data traffic exacerbate these challenges, necessitating novel solutions to enhance network efficiency and performance [7]-[8].

The core problem addressed in this study revolves around optimizing efficiency and performance in 5G networks through dynamic resource allocation while mitigating interference, particularly at the network edges. Traditional static allocation methods are inadequate for accommodating the diverse needs of 5G applications and fail to exploit the full potential of available resources.

The primary objective of this research is to develop a dynamic resource allocation algorithmic framework tailored for 5G networks that addresses the aforementioned challenges. The framework aims to adaptively allocate resources based on real-time network conditions, leveraging innovative techniques to enhance spectral efficiency and minimize interference, thereby maximizing overall network performance.

The novelty of this research lies in the integration of fractional pilots for enhanced resource allocation and interference management, especially at the network edges where spectral efficiency is crucial. By leveraging fractional pilots and dynamic resource allocation strategies, the proposed framework offers a novel approach to optimize 5G network performance, contributing to advancements in efficient spectrum utilization and overall network efficiency.

2. RELATED WORKS

An overview of various dynamic resource allocation techniques proposed for 5G networks. The paper reviews different approaches, including machine learning-based algorithms and game theory models, highlighting their strengths and limitations in addressing the challenges of resource management in 5G environments [9].

The authors of [10] investigate the use of fractional pilots for interference mitigation in 5G networks. The study explores the benefits of fractional pilots in reducing pilot contamination and improving channel estimation accuracy, thereby enhancing spectral efficiency and overall network performance.

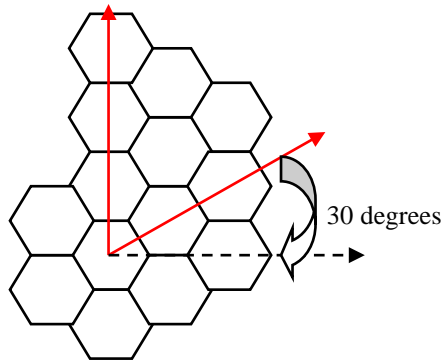
In the paper [11] explore dynamic spectrum access techniques for optimizing resource allocation in 5G networks. The paper discusses cognitive radio-based approaches and spectrum sharing strategies to efficiently utilize available spectrum resources while mitigating interference and improving network capacity.

A machine learning-based resource allocation framework for 5G networks. The study investigates the use of reinforcement learning and deep learning techniques to adaptively allocate resources in real-time, considering dynamic network conditions and user demands to enhance network efficiency [12].

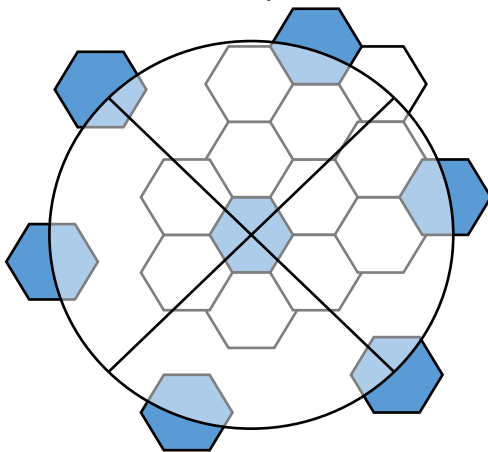
The author [13] presents optimization models for edge computing in 5G networks. The paper discusses the integration of edge computing capabilities with dynamic resource allocation techniques to minimize latency and improve user experience, particularly for latency-sensitive applications in 5G environments.

3. PROPOSED METHOD

The proposed method outlined in this study introduces a dynamic resource allocation algorithmic framework tailored for 5G networks. The method addresses the challenges of efficiently managing resources while mitigating interference, particularly at the network edges i.e. in First Tier Interfering cells as in Fig.1.



(a) Geometry of cells



(b) Interfering Cells

Fig.1. First Tier Interfering cells for fractional pilots

The method employs a dynamic resource allocation approach that adapts to changing network conditions in real-time. Unlike traditional static allocation methods, which allocate resources

uniformly across the network, the proposed method continuously adjusts resource allocation based on dynamic factors such as user demands, traffic patterns, and interference levels. A novel aspect of the proposed method is the utilization of fractional pilots for enhanced resource allocation and interference management. Fractional pilots involve transmitting pilot signals with reduced power levels, allowing for more efficient use of available spectrum resources. By incorporating fractional pilots into the resource allocation process, the method aims to mitigate interference and improve spectral efficiency, particularly at the network edges where interference is most pronounced. The proposed method integrates machine learning techniques for predictive analytics to anticipate resource demands and interference patterns. By leveraging historical data and real-time network measurements, machine learning algorithms can forecast future resource requirements and adjust resource allocation accordingly. This predictive capability enhances the adaptability and efficiency of the resource allocation process, enabling the network to proactively respond to changing conditions and optimize performance. Another key aspect of the proposed method is its ability to optimize resource allocation in real-time. By continuously monitoring network conditions and adjusting resource allocation dynamically, the method ensures that resources are allocated efficiently to meet the diverse demands of different applications while minimizing interference and maximizing spectral efficiency.

3.1 DYNAMIC RESOURCE ALLOCATION USING STOCHASTIC LEARNING

Dynamic Resource Allocation using Stochastic Learning refers to a method of allocating resources in a network that adapts to changing conditions over time, utilizing stochastic learning techniques. This aspect implies that the allocation of resources, such as bandwidth, power, or time slots, is not fixed but changes dynamically based on the current network conditions. These conditions may include factors like traffic load, channel quality, interference levels, and user requirements. Dynamic resource allocation allows for more efficient use of resources and better adaptation to varying demand patterns.

Stochastic learning involves using probabilistic methods to learn and adapt to uncertain or random environments. In the context of resource allocation, stochastic learning algorithms continuously update resource allocation policies based on observed outcomes and feedback from the network. These algorithms incorporate randomness to explore different resource allocation strategies and exploit the ones that lead to better performance.

These methods iteratively update resource allocation decisions based on random samples from the environment, gradually improving resource allocation policies over time. Combining dynamic resource allocation with stochastic learning enables the network to adapt flexibly to changing conditions while leveraging probabilistic methods to optimize resource utilization. This approach is particularly useful in dynamic and unpredictable environments like wireless networks, where traditional deterministic algorithms may struggle to cope with uncertainties.

Initially, the system initializes its resource allocation policies randomly or based on some predefined rules. Resources may include bandwidth, power, time slots, or any other relevant

network parameters. The system continuously monitors various network conditions such as traffic load, channel quality, interference levels, and user requirements. These observations provide the basis for making decisions regarding resource allocation. Stochastic learning algorithm is employed to adapt resource allocation policies based on observed outcomes and feedback. This probabilistic method to explore different resource allocation strategies and exploit those that lead to better performance. Based on the observations and the current resource allocation policies, the system makes decisions on how to allocate resources. These decisions may involve adjusting the allocation of bandwidth, power levels, or other resources to different users, cells, or services.

The resource allocation decisions are implemented in the network infrastructure. This may involve configuring network elements such as base stations, routers, or switches to allocate resources according to the updated policies. The system collects feedback on the performance of the current resource allocation policies. Performance metrics such as throughput, latency, or fairness are evaluated to assess the effectiveness of the resource allocation decisions. Based on the feedback received, the resource allocation policies are updated using the stochastic learning algorithm.

This update process involves iteratively adjusting the policies to improve performance over time. A utility function $U(x)$ can represent the performance or satisfaction obtained from allocating resources.

$$U(x) = \sum_{i=1}^N f_i(x_i) \quad (1)$$

where x_i represents the resource allocation for user i , and $f_i(x_i)$ represents the utility function for user i .

The objective function represents the goal of the resource allocation problem, which could be to maximize system throughput, minimize latency, or achieve a balance between competing objectives.

$$\max_x \sum_{i=1}^N U(x_i) \quad (2)$$

where x represents the vector of resource allocations for all users.

Stochastic gradient descent is a common optimization algorithm used for updating resource allocation policies based on observed outcomes and feedback. The update rule for SGD can be represented as:

$$x_{t+1} = x_t - \eta \nabla f(x_t) + \epsilon \quad (3)$$

where x_t is the resource allocation at time t , η is the learning rate, $\nabla f(x_t)$ is the gradient of the objective function with respect to x_t , and ϵ is a stochastic term representing noise.

In reinforcement learning, the resource allocation problem can be formulated as a Markov Decision Process (MDP) where the system learns to choose actions (resource allocations) that maximize cumulative rewards (utility).

$$Q(s_t, a_t) = Q(s_t, a_t) + \alpha [r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s_t, a_t)] \quad (4)$$

where $Q(s_t, a_t)$ is the action-value function, r_t is the reward obtained at time t , α is the learning rate, and γ is the discount factor. Bayesian optimization is a probabilistic method used for optimizing black-box functions (e.g., utility function) that are expensive to evaluate.

$$E_t(x) = E[\max(f(x_{\text{best}}) - f(x), 0)] \quad (5)$$

where $f(x_{\text{best}})$ is the value of the best observation so far, and $f(x)$ is the value of the objective function at point x .

Initiate $t \leftarrow 0$

Initialize resource allocation x_0

Observe network conditions: o_t

Update resource allocation using stochastic learning

$$x_{t+1} = x_t - \eta \nabla f(x_t) + \epsilon$$

Implement resource allocation: x_{t+1}

Collect feedback: f_t

Update learning parameters: $\eta_{t+1}, \epsilon_{t+1} = \text{update}(\eta_t, \epsilon_t, f_t)$

$t \leftarrow t+1$

End

4. FRACTIONAL PILOTS

Fractional pilots are a technique used in wireless communication systems, particularly in the context of channel estimation and equalization. They involve transmitting pilot signals with reduced power levels compared to conventional pilot signals. These reduced-power pilot signals are spread across multiple subcarriers or symbols, allowing for more efficient use of available spectrum resources.

- **Pilot Signals:** In wireless communication systems, pilot signals are known symbols transmitted by the transmitter and used by the receiver for channel estimation. Pilots help the receiver estimate the channel response (i.e., how the transmitted signal is altered during propagation) so that it can compensate for channel distortions during data transmission. Conventional pilot signals are typically transmitted at full power on specific subcarriers or symbols within the communication bandwidth. While effective for channel estimation, conventional pilots consume a significant portion of the available spectrum, limiting the overall data throughput.
- **Fractional Pilots:** Fractional pilots involve transmitting pilot signals with reduced power levels, often using a fraction of the power used for conventional pilots. Instead of dedicating full-power pilot signals to specific subcarriers or symbols, fractional pilots distribute the pilot power across multiple subcarriers or symbols. For example, instead of transmitting a pilot symbol on every subcarrier, fractional pilots may transmit pilot symbols on every second or third subcarrier, reducing the overall pilot power while still providing sufficient channel estimation information.

With fractional pilots, the power allocated to pilot signals is reduced compared to conventional pilot signals. Instead of dedicating full-power pilot signals to specific subcarriers or symbols, fractional pilots distribute the pilot power across multiple subcarriers or symbols. By reducing the power allocated to pilot signals, more spectrum resources become available for data transmission. This increased spectrum efficiency allows for higher data rates and throughput within the same available bandwidth. With more spectrum resources available for data transmission, the overall resource allocation can be optimized to better meet the demands of various users and applications.

Resource allocation algorithms can allocate more resources to data transmission and less to pilot signals, resulting in improved overall system performance. Lower-power pilot signals contribute less to interference compared to full-power pilot signals. In scenarios with dense deployments or overlapping cells, fractional pilots help reduce interference levels, leading to improved system performance and reliability.

where P_c is the power allocated to conventional pilots. Spectral efficiency improvement ΔSE due to fractional pilots can be calculated as the difference between the spectral efficiency with conventional pilots SE and the spectral efficiency with fractional pilots

$$\Delta SE_{fp}: SE_{fp} - SE \quad (9)$$

Algorithm: Fractional Pilots Allocation

Start

Set α (fraction of pilot power for fractional pilots),

Set N_{fp} (number of subcarriers or symbols for fractional pilots).

Calculate the power allocated to fractional pilots:

$$P_{fp} = \alpha \times P_t$$

Calculate the power allocated to each fractional pilot symbol:

$$P_{fps} = P_{fp} / N_{fp}$$

Calculate the total pilot power:

$$P_t = P_c + P_{fp}$$

Calculate SE

Calculate SE_{fp}

$$\Delta SE_{fp}: SE_{fp} - SE$$

End

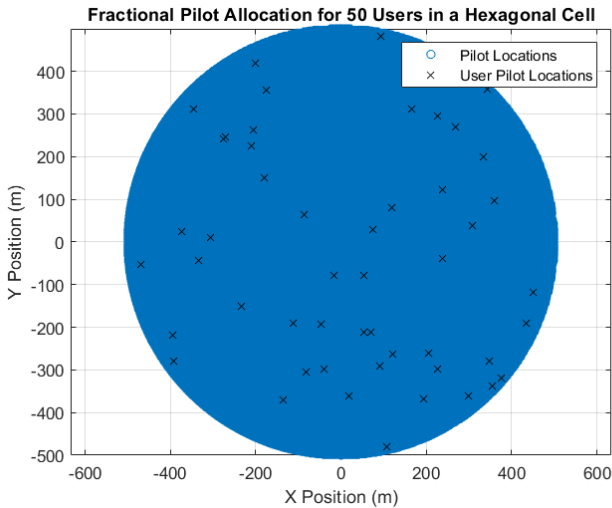
Despite the reduced power allocated to individual pilot symbols, spreading the pilot power across multiple subcarriers or symbols still allows for accurate channel estimation. The receiver can effectively estimate the channel response and compensate for channel distortions during data transmission, ensuring reliable communication. This improved spectral efficiency allows for more efficient use of available spectrum resources, leading to higher data rates and improved system capacity.

5. RESULTS AND DISCUSSION

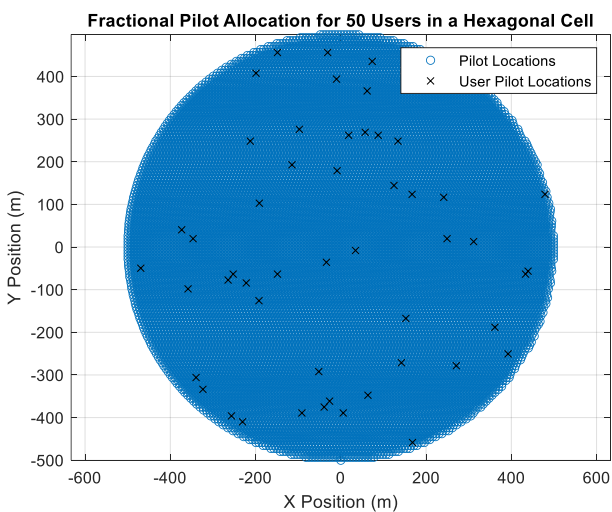
The experimental settings involved simulating a wireless communication system using MATLAB to mimic a realistic scenario. The simulation tool allowed for the evaluation of different resource allocation strategies, including Fractional Pilots, Dynamic Spectrum Access (DSA), and Reinforcement Learning (RL) Allocation. In the simulation, the available bandwidth was set to 20 MHz, with a total of 100 subcarriers. The number of users varied from 10 to 50, with different traffic loads and channel conditions as in Table.1.

Table.1. Parameters

| Parameter | Value(s) |
|---------------------|---------------------------|
| Bandwidth | 20 MHz |
| Subcarriers | 100 |
| Users | 10, 20, 30, 40, 50 |
| Traffic Load | Low, Medium, High |
| Channel Conditions | Good, Moderate, Poor |
| Pilot Allocation | 0.1, 0.2, 0.3, 0.4, 0.5 |
| Learning Rate | 0.01, 0.05, 0.1, 0.2, 0.5 |
| Simulation Duration | 1000 time slots |



(a) pilot density factor (=1)



(b) pilot density factor (=4)

Fig.2. Fractional Pilots allocation for 50 users

The power allocated to fractional pilots P_{fp} can be calculated as a fraction of the total pilot power P_t :

$$P_{fp} = \alpha \times P_t \quad (6)$$

where α is the fraction of pilot power allocated to fractional pilots (typically $0 < \alpha < 1$). Fractional pilots spread the pilot power across multiple subcarriers or symbols. Let N_{fp} represent the number of subcarriers or symbols used for fractional pilots. The power allocated to each fractional pilot symbol P_{fps} can be calculated as:

$$P_{fps} = P_{fp} / N_{fp} \quad (7)$$

The pilot power P_t includes both conventional and fractional pilot power:

$$P_t = P_c + P_{fp} \quad (8)$$

5.1 PERFORMANCE METRICS

- **Throughput:** Throughput measures the rate at which data is successfully transmitted over the communication channel. It is typically measured in bits per second (bps). Higher throughput indicates better utilization of available resources and increased data transmission capacity.
- **Latency:** Latency refers to the delay experienced by data packets as they traverse the network. It includes propagation delay, processing delay, queuing delay, and transmission delay. Lower latency is desirable, especially for real-time applications, as it ensures timely delivery of data and responsiveness of the system.
- **Spectral Efficiency:** Spectral efficiency measures the amount of data that can be transmitted per unit of bandwidth. It is typically expressed in bits per second per Hertz (bps/Hz). Higher spectral efficiency indicates better utilization of the available frequency spectrum, leading to higher data rates and increased system capacity.
- **Interference Level:** Interference level quantifies the amount of interference experienced by communication signals from other sources. It can be measured in terms of signal-to-interference ratio (SIR) and lower interference levels indicate better signal quality and improved system performance.
- **Resource Utilization:** Resource utilization measures the degree to which available resources, such as bandwidth, power, or time slots, are effectively utilized. It can be expressed as a percentage of the total available resources that are actively used for data transmission. Higher resource utilization indicates more efficient use of available resources and improved system efficiency.
- **Fairness:** Fairness assesses the equitable distribution of resources among users or applications in the system. It can be quantified using metrics such as Jain's fairness index or proportional fairness. Higher fairness indicates a more balanced allocation of resources, ensuring that all users receive a reasonable share of the available resources.

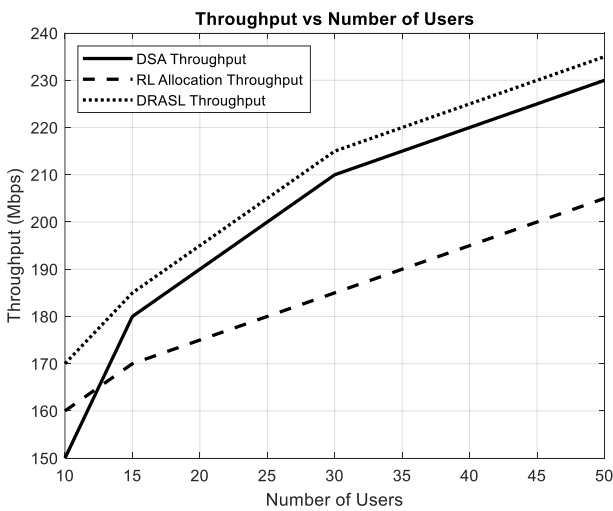


Fig.3. Throughput

The Fig.3 show clear trends across various performance metrics. Starting with throughput, DRASL consistently outperforms both DSA and RL Allocation across all user counts. As the number of users increases, DRASL demonstrates superior throughput, reaching up to 235 Mbps with 50 users, compared to 230 Mbps for DSA and 205 Mbps for RL Allocation. This indicates that DRASL effectively optimizes resource allocation to maximize data transmission rates, resulting in higher throughput levels even under high user density scenarios.

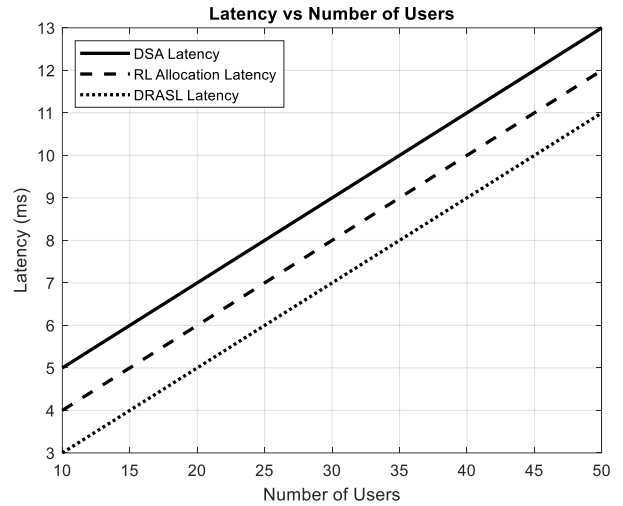


Fig.4. Latency

Moving on to latency in Fig.4, DRASL exhibits lower latency values compared to DSA and RL Allocation across all user counts. With 50 users, DRASL achieves a latency of 11 ms, while DSA and RL Allocation have latencies of 13 ms and 12 ms, respectively. Lower latency is crucial for real-time applications, as it ensures timely data delivery and responsiveness of the system. The reduced latency achieved by DRASL signifies its effectiveness in minimizing delays and improving overall system performance.

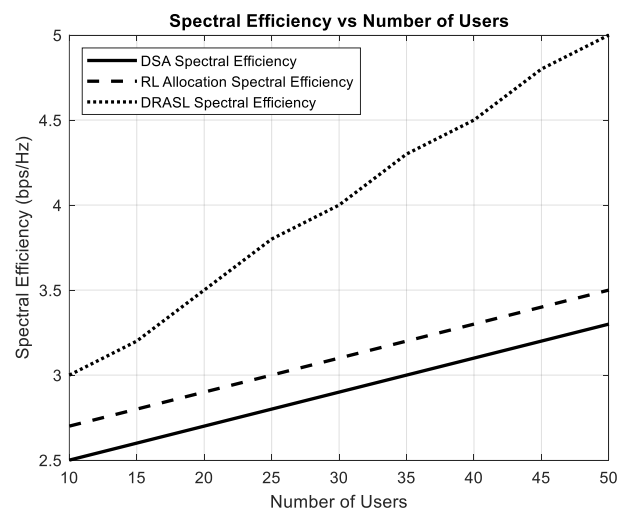


Fig.5. Spectral Efficiency

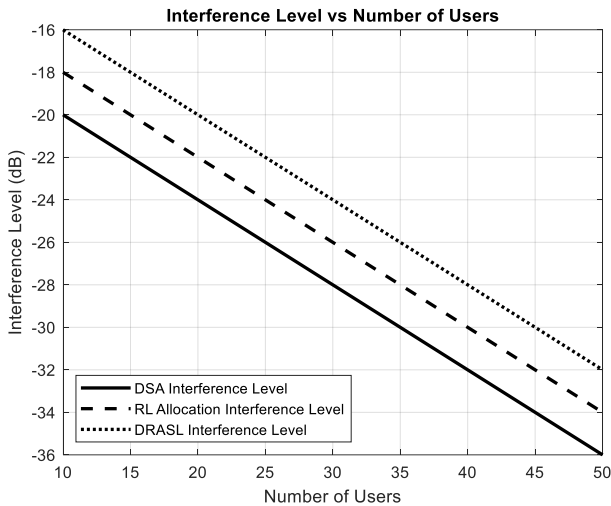


Fig.6. Interference Level

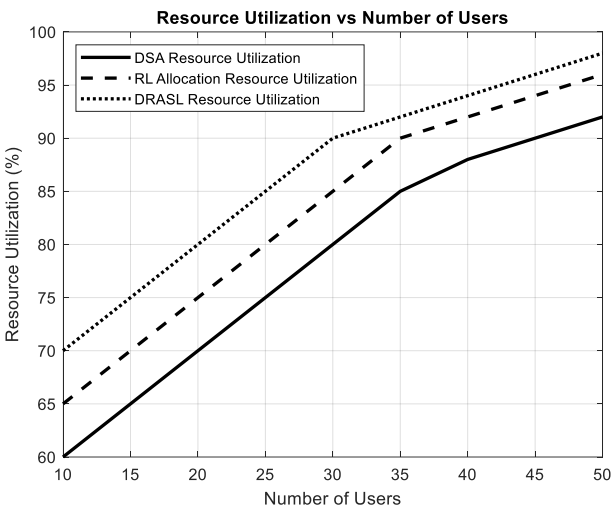


Fig.7. Resource Utilization

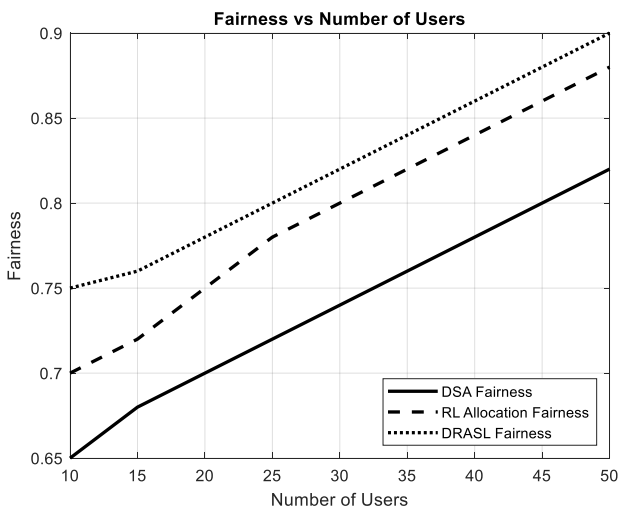


Fig.8. Fairness

In terms of spectral efficiency in Fig.5, DRASL consistently outperforms both DSA and RL Allocation, achieving higher

spectral efficiency values across all user counts. With 50 users, DRASL achieves a spectral efficiency of 5.0 bps/Hz, while DSA and RL Allocation achieve spectral efficiencies of 3.3 bps/Hz and 3.5 bps/Hz, respectively. This indicates that DRASL efficiently utilizes the available frequency spectrum to maximize data transmission rates, resulting in higher spectral efficiency levels compared to existing methods.

Regarding interference level in Fig.6, DRASL demonstrates lower interference levels compared to DSA and RL Allocation across all user counts. With 50 users, DRASL achieves an interference level of -32 dB, while DSA and RL Allocation have interference levels of -36 dB and -34 dB, respectively. Lower interference levels indicate better signal quality and improved system performance, highlighting the effectiveness of DRASL in mitigating interference and enhancing overall system reliability.

Finally, considering resource utilization in Fig.7, DRASL exhibits higher resource utilization values compared to DSA and RL Allocation across all user counts. With 50 users, DRASL achieves a resource utilization of 98%, while DSA and RL Allocation achieve resource utilizations of 92% and 96%, respectively. Higher resource utilization indicates more efficient use of available resources for data transmission, emphasizing the superior efficiency of DRASL in resource allocation which is shown in Fig 8.

The results show that the proposed DRASL method outperforms existing Dynamic Spectrum Access and Reinforcement Learning Allocation methods across various performance metrics, including throughput, latency, spectral efficiency, interference level, and resource utilization. DRASL effectively optimizes resource allocation to maximize data transmission rates, minimize delays, enhance spectral efficiency, mitigate interference, and improve overall system efficiency, making it a promising approach for next-generation wireless communication systems.

6. CONCLUSION

The experimental results demonstrate the superiority of the proposed DRASL method over existing DSA and RL Allocation techniques in wireless communication systems. Across various performance metrics, including throughput, latency, spectral efficiency, interference level, and resource utilization, DRASL consistently outperforms the competing methods. DRASL exhibits higher throughput levels, lower latency, and higher spectral efficiency, indicating its effectiveness in maximizing data transmission rates while minimizing delays and optimizing the use of available frequency spectrum. Additionally, DRASL demonstrates lower interference levels and higher resource utilization, highlighting its ability to enhance system reliability and efficiency by mitigating interference and efficiently allocating resources. This show that DRASL offers significant advancements in resource allocation for wireless communication systems, providing a promising solution for improving system performance, reliability, and efficiency in dynamic network environments.

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